

# Heterotic Supersymmetry: the Legacy of $D = 10$ and $N = 4$

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# A Zip code for MSSM fields

## Localization properties of quarks, leptons and Higgses

- Higgs bosons and top-quark in the “bulk” lead to large top-quark Yukawa coupling
- first 2 families localized (exhibiting family symmetries)

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## The legacy of higher dimensions

- Mirage Mediation (compressed spectrum for gauginos)
- Natural Susy
- discrete (nonabelian) family symmetries

Remnants of  $N=4$  SUSY from higher dimensions that might hide Susy at the LHC!

# Guidelines

- **Spinors if  $SO(10)$**  might be important even in absence of GUT gauge group
- gauge-top Yukawa unification in the MSSM
- presence of **discrete symmetries** with many applications

(Kobayashi, HPN, Ploeger, Raby, Ratz, 2006)

# Guidelines

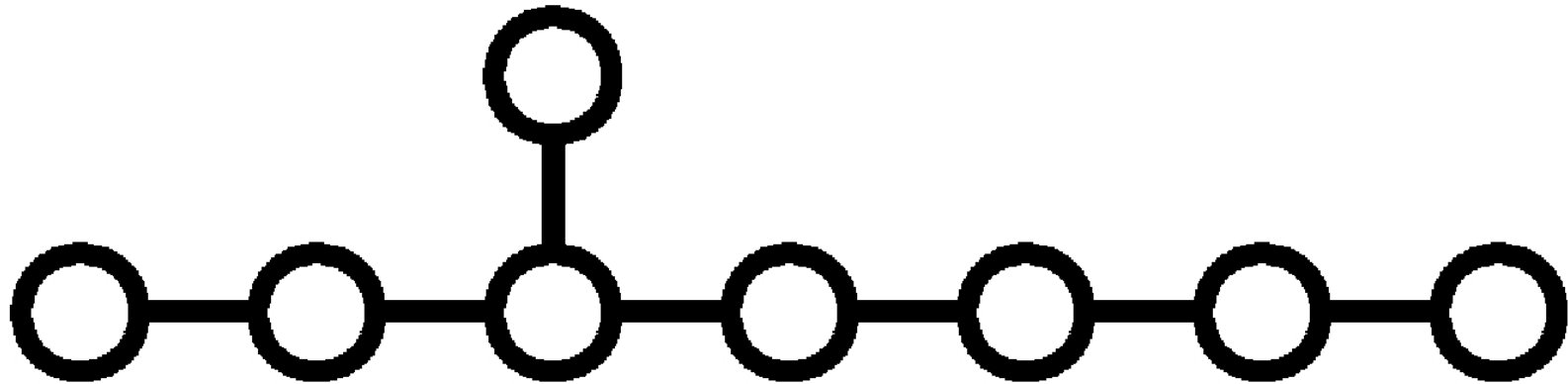
- **Spinors** if **SO(10)** might be important even in absence of GUT gauge group
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(Kobayashi, HPN, Ploeger, Raby, Ratz, 2006)

From the mathematical structure we might prefer exceptional groups

- There is a maximal group:  $E_8$ ,
- but  $E_8$  and  $E_7$  do not allow chiral fermions in  $d = 4$ .
- **How does this fit with our usual picture of unification based on SU(5) or SO(10)?**

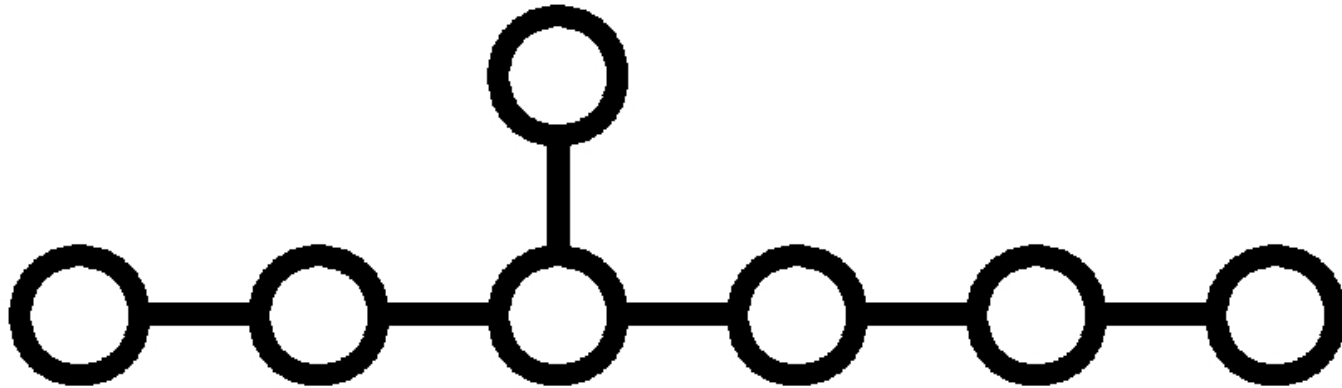
# Maximal Group



$E_8$  is the maximal group.

There are, however, no chiral representations in  $d = 4$ .

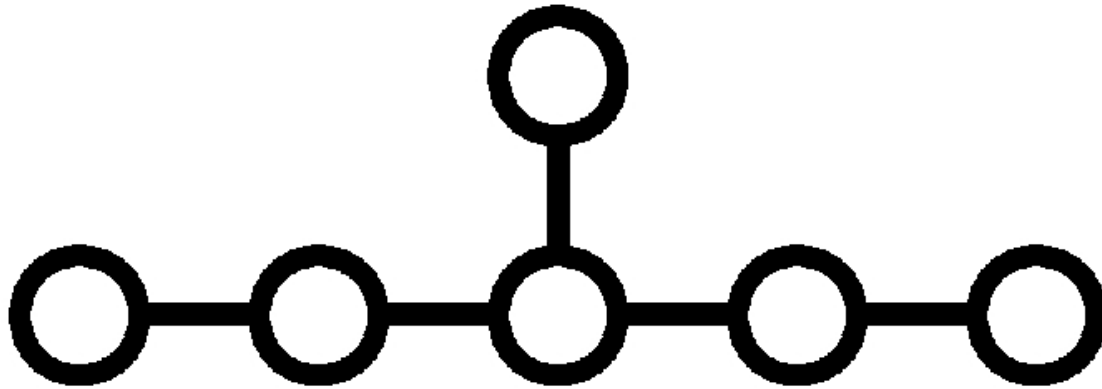
$E_7$



Next smaller is  $E_7$ .

No chiral representations in  $d = 4$  either

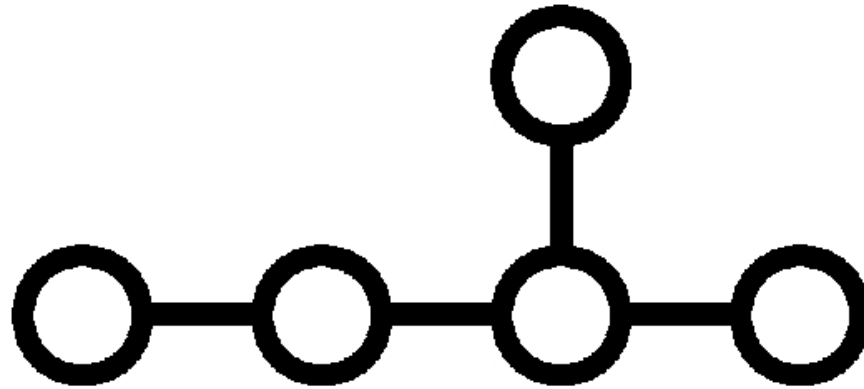
$E_6$



$E_6$  allows for chiral representations even in  $d = 4$ .



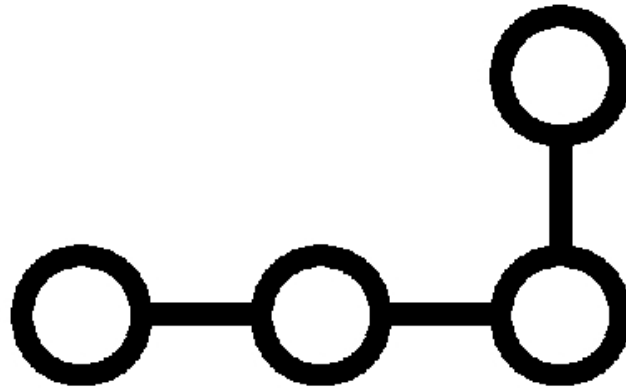
$$E_5 = D_5$$



$E_5$  is usually not called exceptional.

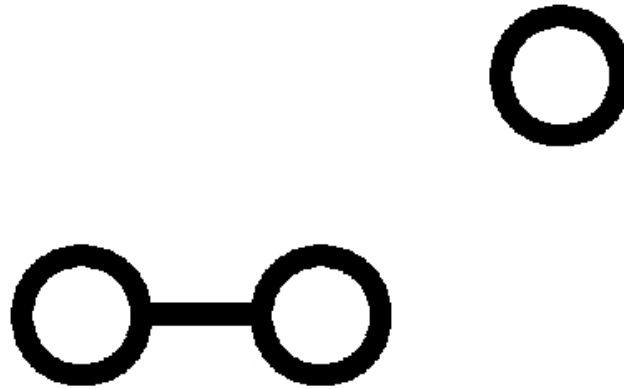
It coincides with  $D_5 = SO(10)$ .

$$E_4 = A_4$$



$E_4$  coincides with  $A_4 = SU(5)$

$E_3$



$E_3$  coincides with  $A_2 \times A_1$  which is  $SU(3) \times SU(2)$ .

# Exceptional groups in string theory

String theory “favours”  $E_8$

- $E_8 \times E_8$  heterotic string
- $E_8$  enhancement as a nonperturbative effect (M- or F-theory)

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Strings live in higher dimensions:

- chiral spectrum possible even with  $E_8$
- $E_8$  broken in process of compactification
- provides source for (nonabelian) discrete symmetries
- from  $E_8/SO(10)$  and  $SO(6)$  of the higher dimensional Lorentz group

# Geography

Many properties of the models depend on the geography of extra dimensions, such as

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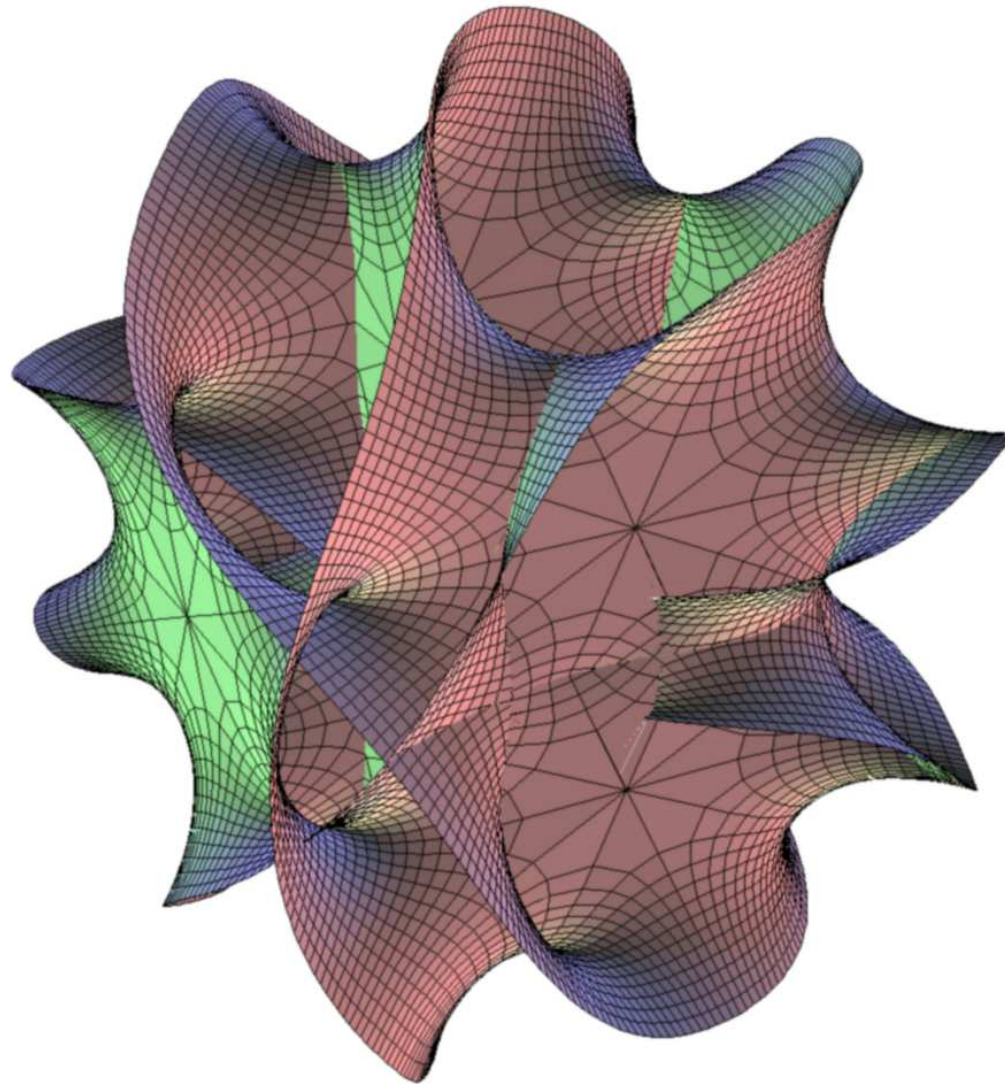
- the **location** of quarks and leptons,
- the **relative location** of Higgs bosons,

but there is also a “localization” of gauge fields

- $E_8 \times E_8$  in the bulk
- smaller gauge groups on various branes

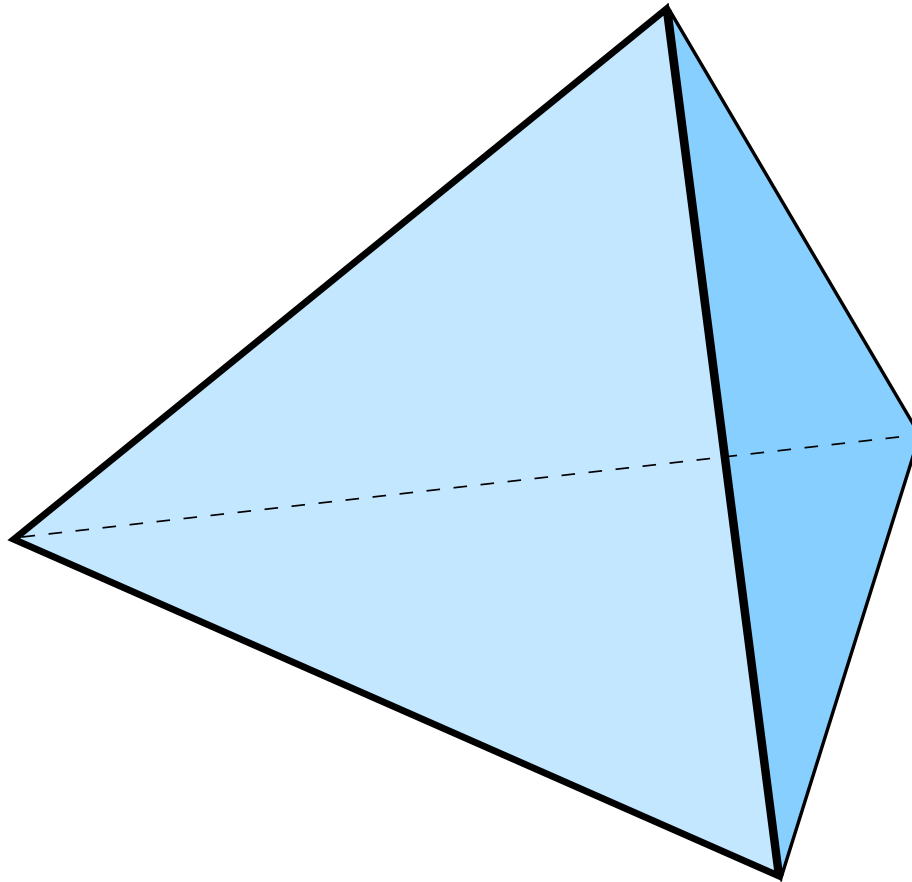
Observed 4-dimensional gauge group is common subgroup of the various localized gauge groups!

# Calabi Yau Manifold





# Orbifold



(Dixon, Harvey, Vafa, Witten, 1985)

# Berechenbarkeit

We need calculability that goes beyond the effective supergravity field theory approach, e.g. in the form exact conformal field theory. This requires:

- perturbative string theory
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- perturbative string theory
- explicit knowledge of metric of the manifold

Approximations corresponds to points of enhanced symmetries and enhanced particle spectra

- slightly broken symmetries (Frogatt-Nielsen) provide
- small parameters that appear in particle physics

Hopefully nature is close to points with full calculability.

# Enhanced symmetries

This approximate scheme allows model building with geometric intuition. Sectors might exhibit

- enhanced gauge and discrete symmetries
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If we move away from these points of enhanced calculability, we might still keep “Berechenbarkeit”

- sectors with  $N = 4$  or  $N = 2$  supersymmetry
- conformal field theory calculations still useful after “blow-up”
- special role of the Green-Schwarz anomaly polynomial.

(Blaszczyk, Cabo, HPN, Ruehle, 2011)

# Localization

Quarks, Leptons and Higgs fields can be localized:

- in the Bulk ( $d = 10$  **untwisted** sector)
- on 3-Branes ( $d = 4$  twisted sector **fixed points**)
- on 5-Branes ( $d = 6$  twisted sector **fixed tori**)

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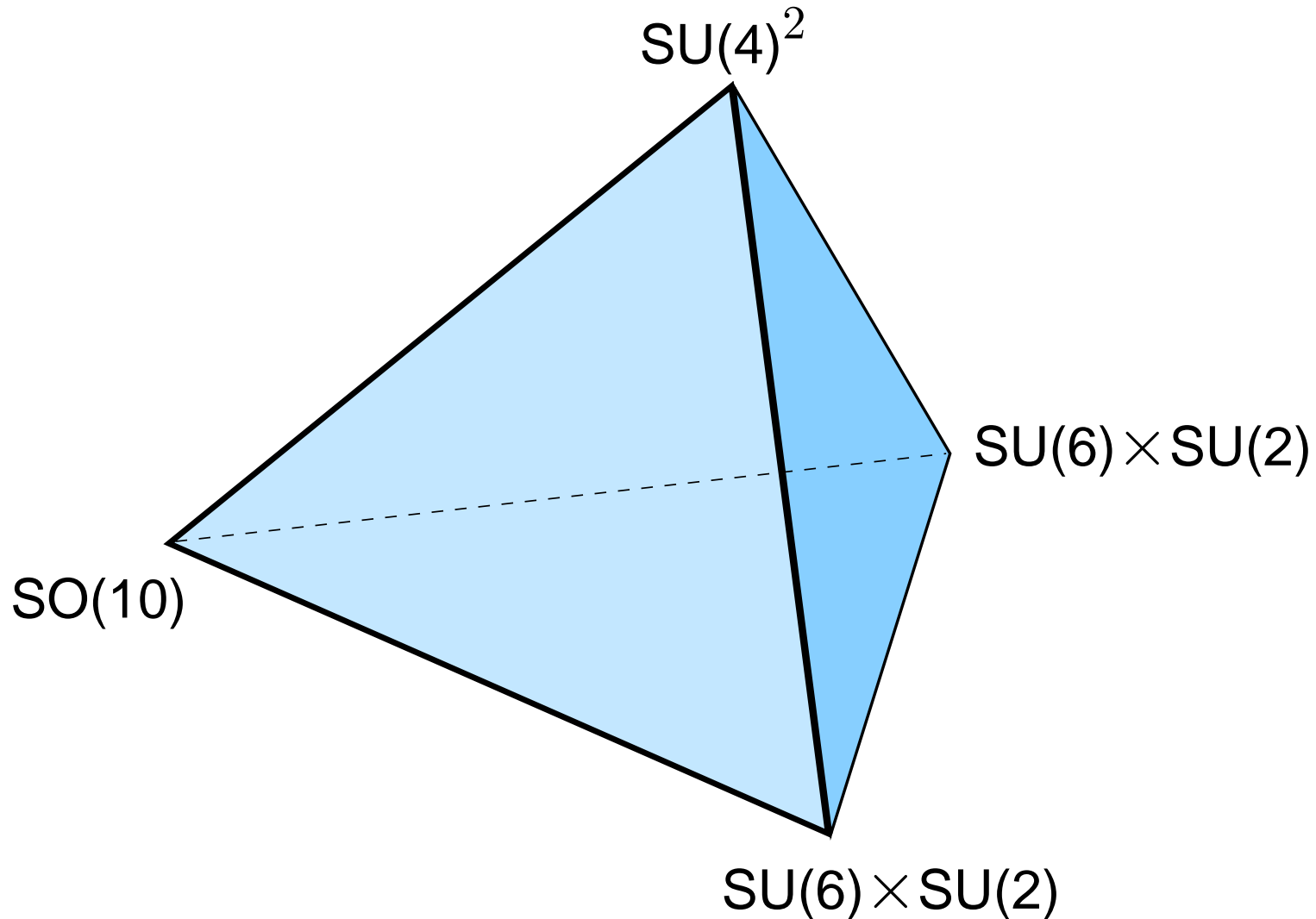
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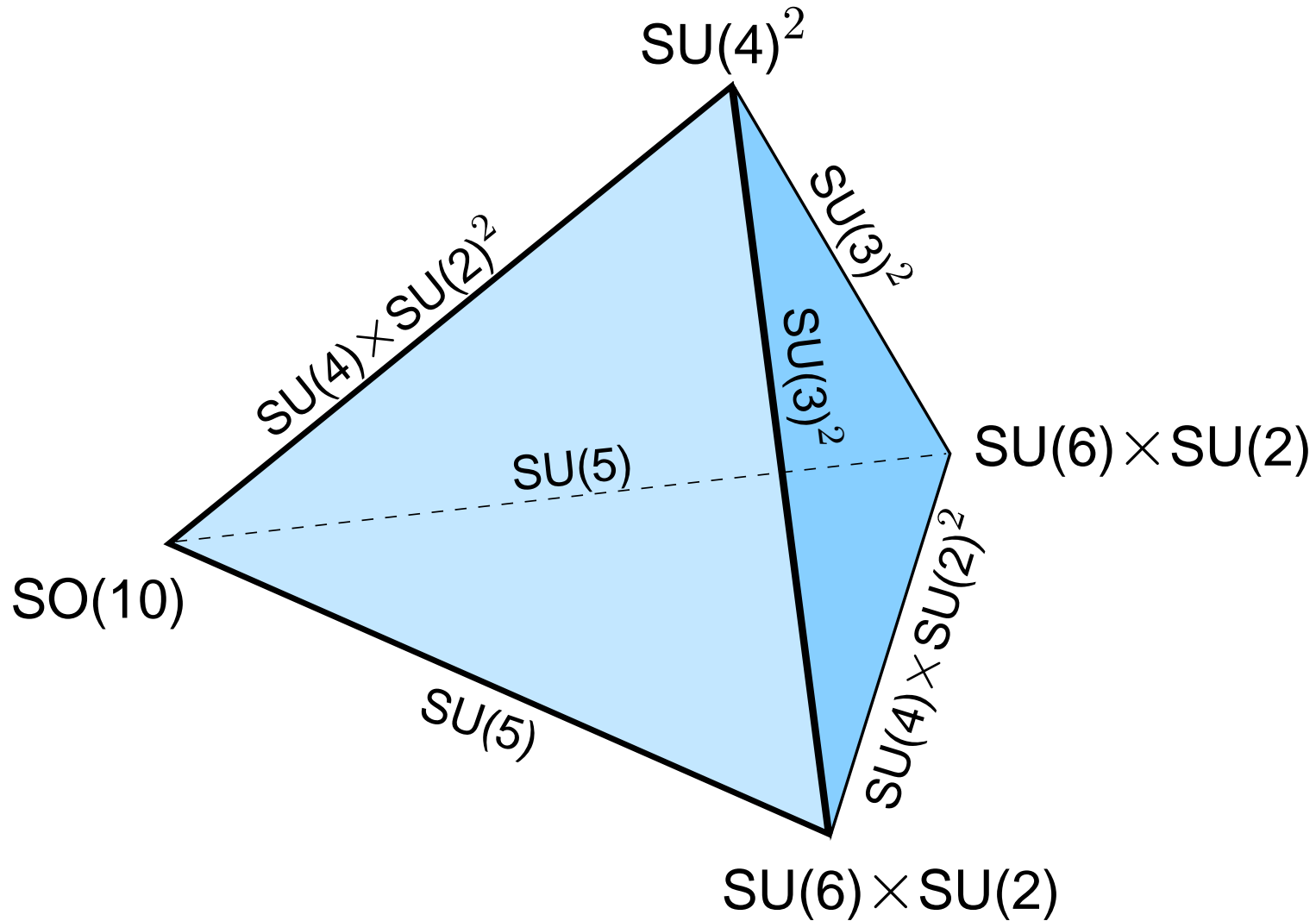
# Localized gauge symmetries



(Förste, HPN, Vaudrevange, Wingerter, 2004)



# Standard Model Gauge Group



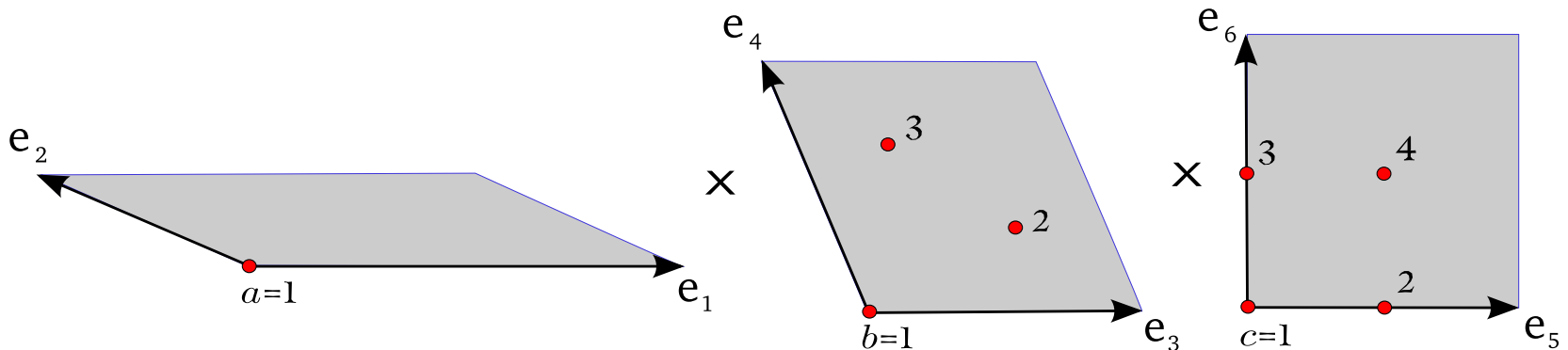
# The MiniLandscape

- many models with the **exact spectrum of the MSSM** (absence of chiral exotics)  
(Lebedev, HPN, Raby, Ramos-Sanchez, Ratz, Vaudrevange, Wingerter, 2006-2009)
- **family symmetries for the first two families**  
(Kobayashi, HPN, Ploeger, Raby, Ratz, 2006)
- gauge- and (partial) Yukawa unification  
(Raby, Wingerter, 2007)
- **large top quark Yukawa coupling**
- models with **R-parity** + solution to the  **$\mu$ -problem**  
(Lebedev, HPN, Raby, Ramos-Sanchez, Ratz, Vaudrevange, Wingerter, 2007)
- gaugino condensation and **mirage mediation**  
(Löwen, HPN, 2008)

# Sectors

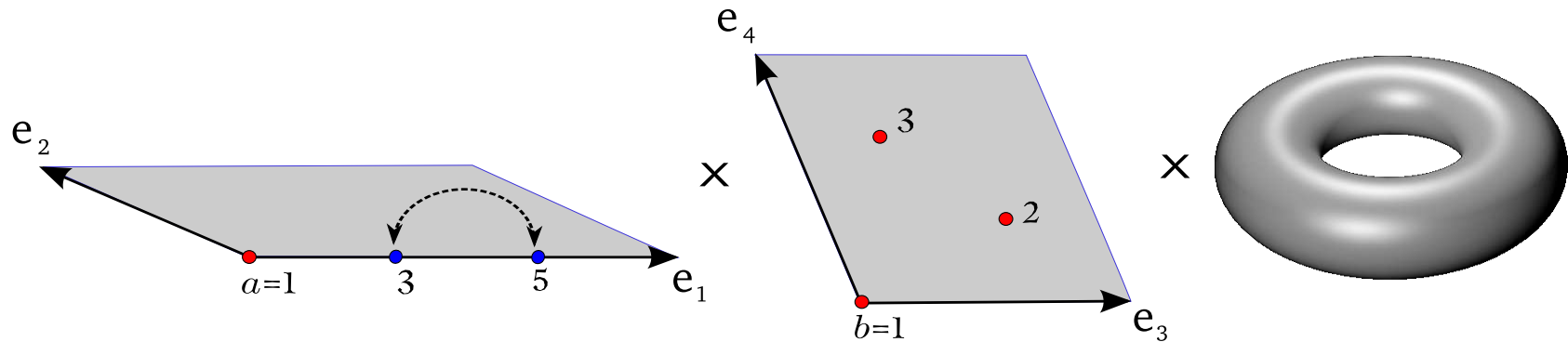
The underlying  $Z_6II$  orbifold has the following sectors:

- the untwisted sector ( bulk  $D = 10$ ,  $N = 4$  Susy)
- three twisted sectors corresponding to  $\theta$ ,  $\theta^2$  and  $\theta^3$



The  $\theta$  sector has  $4 \times 3 = 12$  fixed points, corresponding to “3-branes” confined to  $D=4$  space-time ( $N = 1$  Susy).

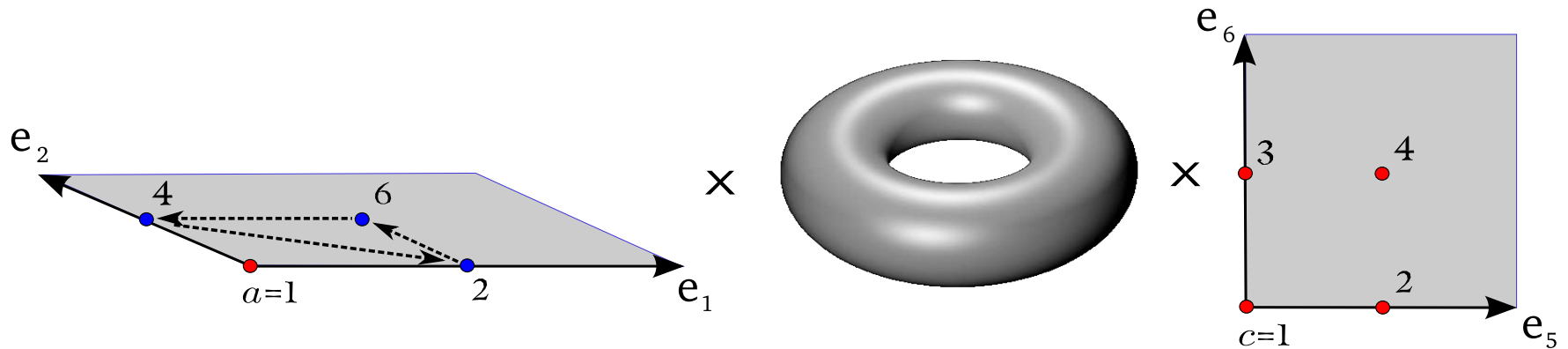
# $\theta^2$ twisted sector



The  $\theta^2$  sector contains  $2 \times 3$  fixed tori corresponding to

- “5-branes” confined to 6 space-time dimensions (remnants of  $N = 2$  Susy)

# $\theta^3$ twisted sector



The  $\theta^3$  sector contains  $2 \times 4$  fixed tori:

- “5-branes” confined to 6 space-time dimensions (sector with  $N = 2$  Susy)

Where do we find quarks, leptons and Higgs bosons in the models of the MiniLandscape?

# A Benchmark Model

At the orbifold point the gauge group is

$$SU(3) \times SU(2) \times U(1)^9 \times SU(4) \times SU(2)$$

- one  $U(1)$  is anomalous
- there are singlets and vectorlike exotics
- decoupling of exotics and breakdown of gauge group has been verified
- remaining gauge group

$$SU(3) \times SU(2) \times U(1)_Y \times SU(4)_{\text{hidden}}$$

- for discussion of neutrinos and R-parity we keep also the  $U(1)_{B-L}$  charges

# Spectrum

#	irrep	label	#	irrep	label
3	$(\mathbf{3}, \mathbf{2}; \mathbf{1}, \mathbf{1})_{(1/6, 1/3)}$	$q_i$	3	$(\bar{\mathbf{3}}, \mathbf{1}; \mathbf{1}, \mathbf{1})_{(-2/3, -1/3)}$	$\bar{u}_i$
3	$(\mathbf{1}, \mathbf{1}; \mathbf{1}, \mathbf{1})_{(1, 1)}$	$\bar{e}_i$	8	$(\mathbf{1}, \mathbf{2}; \mathbf{1}, \mathbf{1})_{(0, *)}$	$m_i$
3 + 1	$(\bar{\mathbf{3}}, \mathbf{1}; \mathbf{1}, \mathbf{1})_{(1/3, -1/3)}$	$\bar{d}_i$	1	$(\mathbf{3}, \mathbf{1}; \mathbf{1}, \mathbf{1})_{(-1/3, 1/3)}$	$d_i$
3 + 1	$(\mathbf{1}, \mathbf{2}; \mathbf{1}, \mathbf{1})_{(-1/2, -1)}$	$l_i$	1	$(\mathbf{1}, \mathbf{2}; \mathbf{1}, \mathbf{1})_{(1/2, 1)}$	$\bar{l}_i$
1	$(\mathbf{1}, \mathbf{2}; \mathbf{1}, \mathbf{1})_{(-1/2, 0)}$	$h_d$	1	$(\mathbf{1}, \mathbf{2}; \mathbf{1}, \mathbf{1})_{(1/2, 0)}$	$h_u$
6	$(\bar{\mathbf{3}}, \mathbf{1}; \mathbf{1}, \mathbf{1})_{(1/3, 2/3)}$	$\bar{\delta}_i$	6	$(\mathbf{3}, \mathbf{1}; \mathbf{1}, \mathbf{1})_{(-1/3, -2/3)}$	$\delta_i$
14	$(\mathbf{1}, \mathbf{1}; \mathbf{1}, \mathbf{1})_{(1/2, *)}$	$s_i^+$	14	$(\mathbf{1}, \mathbf{1}; \mathbf{1}, \mathbf{1})_{(-1/2, *)}$	$s_i^-$
16	$(\mathbf{1}, \mathbf{1}; \mathbf{1}, \mathbf{1})_{(0, 1)}$	$\bar{n}_i$	13	$(\mathbf{1}, \mathbf{1}; \mathbf{1}, \mathbf{1})_{(0, -1)}$	$n_i$
5	$(\mathbf{1}, \mathbf{1}; \mathbf{1}, \mathbf{2})_{(0, 1)}$	$\bar{\eta}_i$	5	$(\mathbf{1}, \mathbf{1}; \mathbf{1}, \mathbf{2})_{(0, -1)}$	$\eta_i$
10	$(\mathbf{1}, \mathbf{1}; \mathbf{1}, \mathbf{2})_{(0, 0)}$	$h_i$	2	$(\mathbf{1}, \mathbf{2}; \mathbf{1}, \mathbf{2})_{(0, 0)}$	$y_i$
6	$(\mathbf{1}, \mathbf{1}; \mathbf{4}, \mathbf{1})_{(0, *)}$	$f_i$	6	$(\mathbf{1}, \mathbf{1}; \bar{\mathbf{4}}, \mathbf{1})_{(0, *)}$	$\bar{f}_i$
2	$(\mathbf{1}, \mathbf{1}; \mathbf{4}, \mathbf{1})_{(-1/2, -1)}$	$f_i^-$	2	$(\mathbf{1}, \mathbf{1}; \bar{\mathbf{4}}, \mathbf{1})_{(1/2, 1)}$	$\bar{f}_i^+$
4	$(\mathbf{1}, \mathbf{1}; \mathbf{1}, \mathbf{1})_{(0, \pm 2)}$	$\chi_i$	32	$(\mathbf{1}, \mathbf{1}; \mathbf{1}, \mathbf{1})_{(0, 0)}$	$s_i^0$
2	$(\bar{\mathbf{3}}, \mathbf{1}; \mathbf{1}, \mathbf{1})_{(-1/6, 2/3)}$	$\bar{v}_i$	2	$(\mathbf{3}, \mathbf{1}; \mathbf{1}, \mathbf{1})_{(1/6, -2/3)}$	$v_i$

# The location of Higgs bosons

Typically there could be a multitude of Higgs doublets (and triplets) in the spectrum

- triplets heavy or projected out
- exactly two Higgs doublet multiplets should remain light
- all other heavy

This is the so-called  $\mu$  problem



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The MiniLandscape identifies exactly one Higgs pair protected by a discrete R-symmetry and provides a unique solution to the  $\mu$  problem, because the

Higgs bosons live in the untwisted sector (delocalized Higgs as in torus compactification: remnants of  $N = 4$  susy)

# Location of top quark

Given the fact that the Higgs multiplets live in the bulk we now explore how to obtain a large top quark Yukawa coupling

- need maximum “overlap” with the Higgs multiplet
- results of the MiniLandscape teach us that this requires the **top quark to live in the untwisted sector** as well

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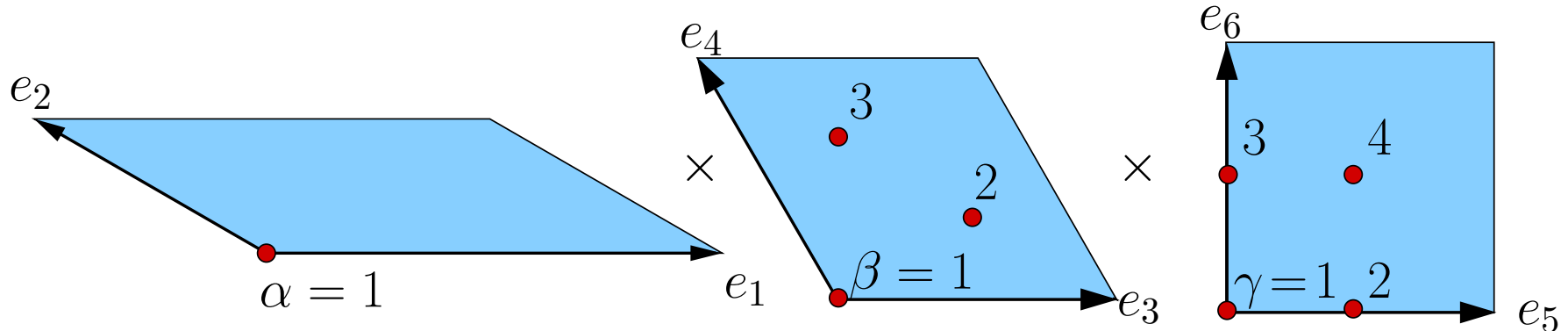
**Top quark in untwisted sector (bulk).** The third family is usually distributed over various sectors (it is not in a complete localized  $SO(10)$  representation).

Side remark:

3 “complete” families impossible within  $Z_6II$  orbifold

# First and second family

The first and second families are in complete localized 16-dimensional representation of  $SO(10)$  (at points of “enhanced” gauge symmetry)

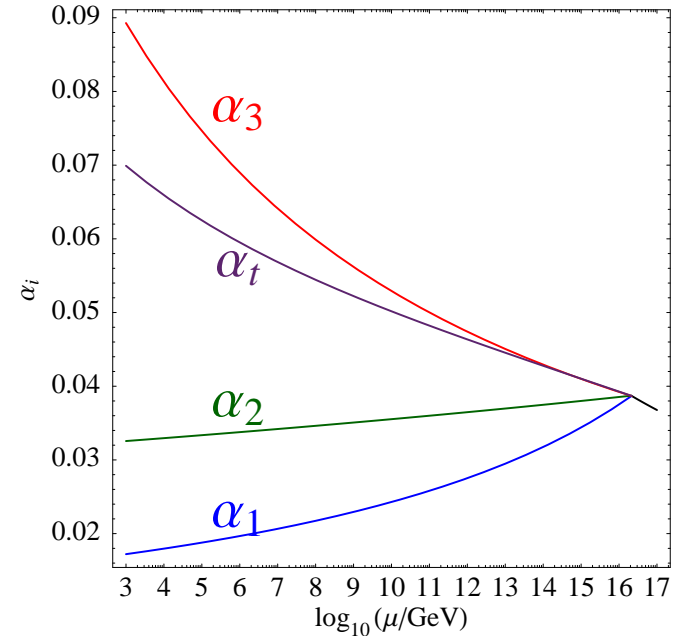


They live in the  $\theta$  twisted sector and are localized at the fixed points  $\alpha = 1, \beta = 1, \gamma = 1, 3$

exhibiting a  $D_4$  family symmetry.

# Unification

- Higgs doublets live in the **bulk**
- **heavy top quark live in the bulk as well.**
- $\mu$ -term protected by a **discrete R-symmetry**



- Minkowski vacuum before Susy breakdown (no AdS)
- **solution to  $\mu$ -problem** (Casas, Munoz, 1993)
- **first two families localized (smaller Yukawa couplings) exhibiting a discrete family symmetry**

# Emergent localization properties

The benchmark model illustrates some of the general properties of the MiniLandscape

- exactly two Higgs multiplets (no triplets)
- the top quark lives in the untwisted sector (as well as the Higgs multiplets)
- only one trilinear Yukawa coupling (all others suppressed)

# Emergent localization properties

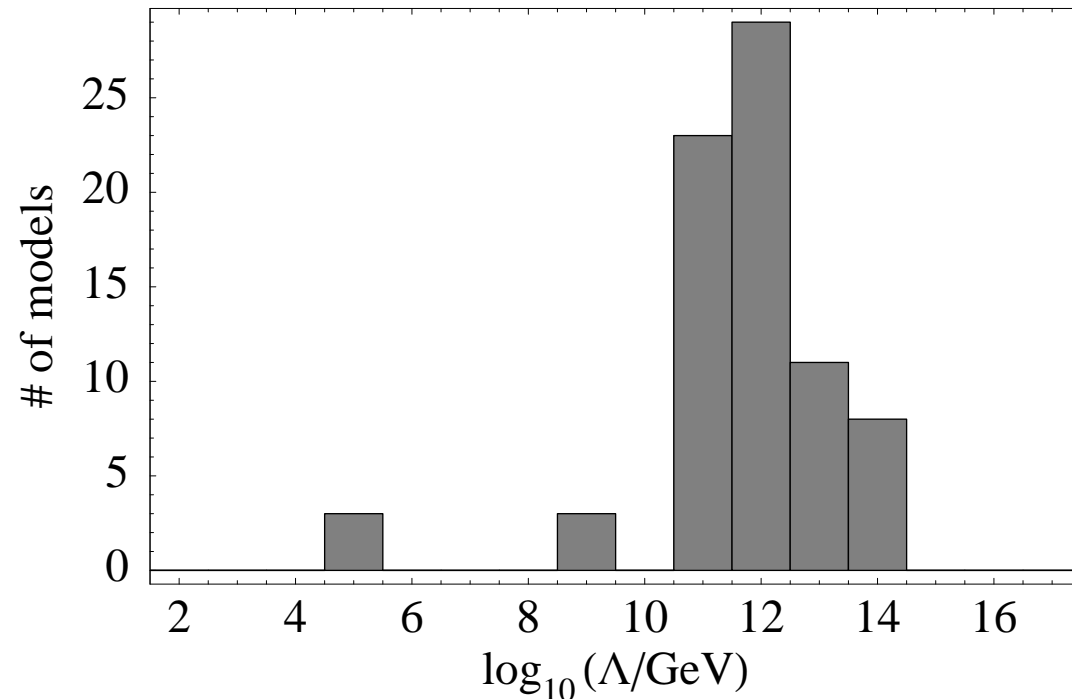
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The fact that the top-quark has this unique property among all the quarks and leptons has important consequences for the phenomenological predictions including supersymmetry breakdown.

(Krippendorff, HPN, Ratz, Winkler, 2012)

# Heterotic string: gaugino condensation



Gravitino mass  $m_{3/2} = \Lambda^3 / M_{\text{Planck}}^2$  and  $\Lambda \sim \exp(-\tau)$

SU(4) in hidden sector predicts gravitino mass in TeV range

(Lebedev, HPN, Raby, Ramos-Sanchez, Ratz, Vaudrevange, Wingerter, 2006)



# Mirage scheme

In string theory we have (from **flux** and **gaugino condensate**)

$$W = \text{flux} - \exp(-X)$$

- modulus mediation suppressed  
(in the process of adjusting the vacuum energy)  
 $X \sim \log(M_{\text{Planck}}/m_{3/2}) \sim 4\pi^2$
- radiative corrections become relevant ( $\beta$  function)
- Mixed mediation scheme: **Mirage Mediation (MMAM)**  
**with mirage pattern for gaugino masses:**  
 $m_{1/2} \sim m_{3/2}/4\pi^2$  (Choi, Falkowski, Nilles, Olechowski, 2005)

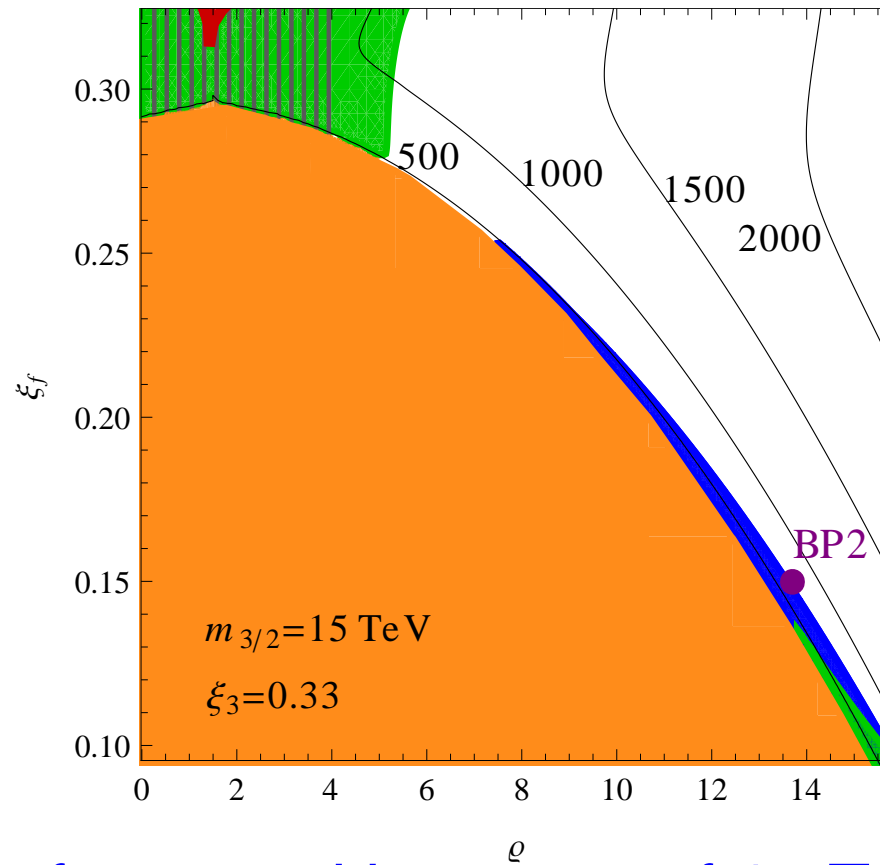
generic in the framework of Type IIB and heterotic theory.

# The overall pattern

This provides a specific pattern for the soft masses with a large gravitino mass in the multi-TeV range

- normal squarks and sleptons in Multi-TeV range
- top squarks ( $\tilde{t}_L, \tilde{b}_L$ ) and  $\tilde{t}_R$  in TeV-range  
(suppressed by  $\log(M_{\text{Planck}}/m_{3/2}) \sim 4\pi^2$ )
- A-parameters in TeV range
- gaugino masses in TeV range
- mirage pattern for gaugino masses  
(compressed spectrum)
- heavy moduli (enhanced by  $\log(M_{\text{Planck}}/m_{3/2})$   
compared to the gravitino mass)

# Benchmark model

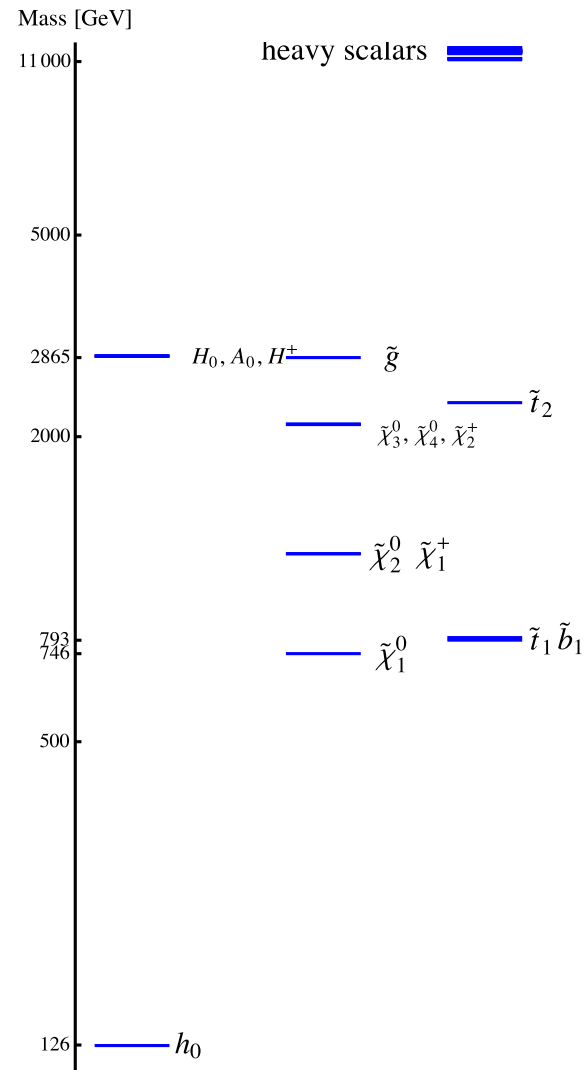


Parameter scan for a gravitino mass of 15 TeV.

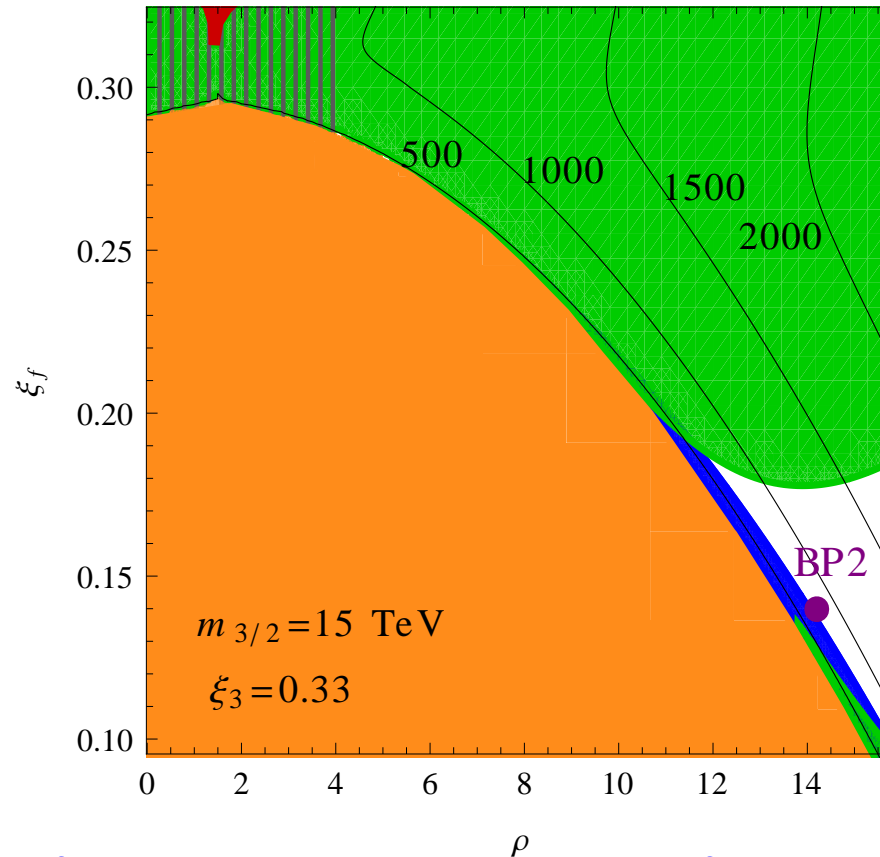
The coloured regions are excluded while the hatched region indicates the current reach of the LHC.

The contours indicate the mass of the lightest stop.

# Spectrum



# After Higgs discovery



Parameter scan for a gravitino mass of 15 TeV.

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# Messages

- large gravitino mass (multi TeV-range)
- gaugino masses and stops suppressed by  $\log(M_{\text{Planck}}/m_{3/2})$
- other sfermion masses are of order  $m_{3/2}$
- the heterotic string yields “Natural SUSY” as a remnant of the underlying  $N = 4$  Susy
  - mirage pattern for gauginos,
  - light stop masses
- and this is a severe challenge for LHC searches.

# Conclusions

## Localization of quarks, leptons and Higgs bosons

- realistic models require Higgs multiplets and top multiplets in **bulk** (connected to  $\mu$  problem)
- this implies Gauge-Yukawa unification
- other fields tend to be localized at fixed points (tori) and exhibit discrete family symmetries

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## The legacy from extra dimensions ( $D = 10$ )

- discrete family symmetries
- mirage mediation (a hierarchy from  $\log(M_{\text{Planck}}/m_{3/2})$ )
- mass spectrum of “**Natural Susy**” from  $N = 4$



# Heterotic supersymmetry

is more than just  $N = 1$  Susy in  $D = 4$ .

It provides the Zip code for the MSSM fields,

- Higgs boson are bulk fields with enhanced susy
- R-symmetries for  $\mu$ -problem and proton stability
- Gauge-Higgs unification (continuous Wilson lines, shift symmetry of the Kaehler potential)
- top quark as bulk field: gauge-top unification
- discrete (nonabelian) family symmetries

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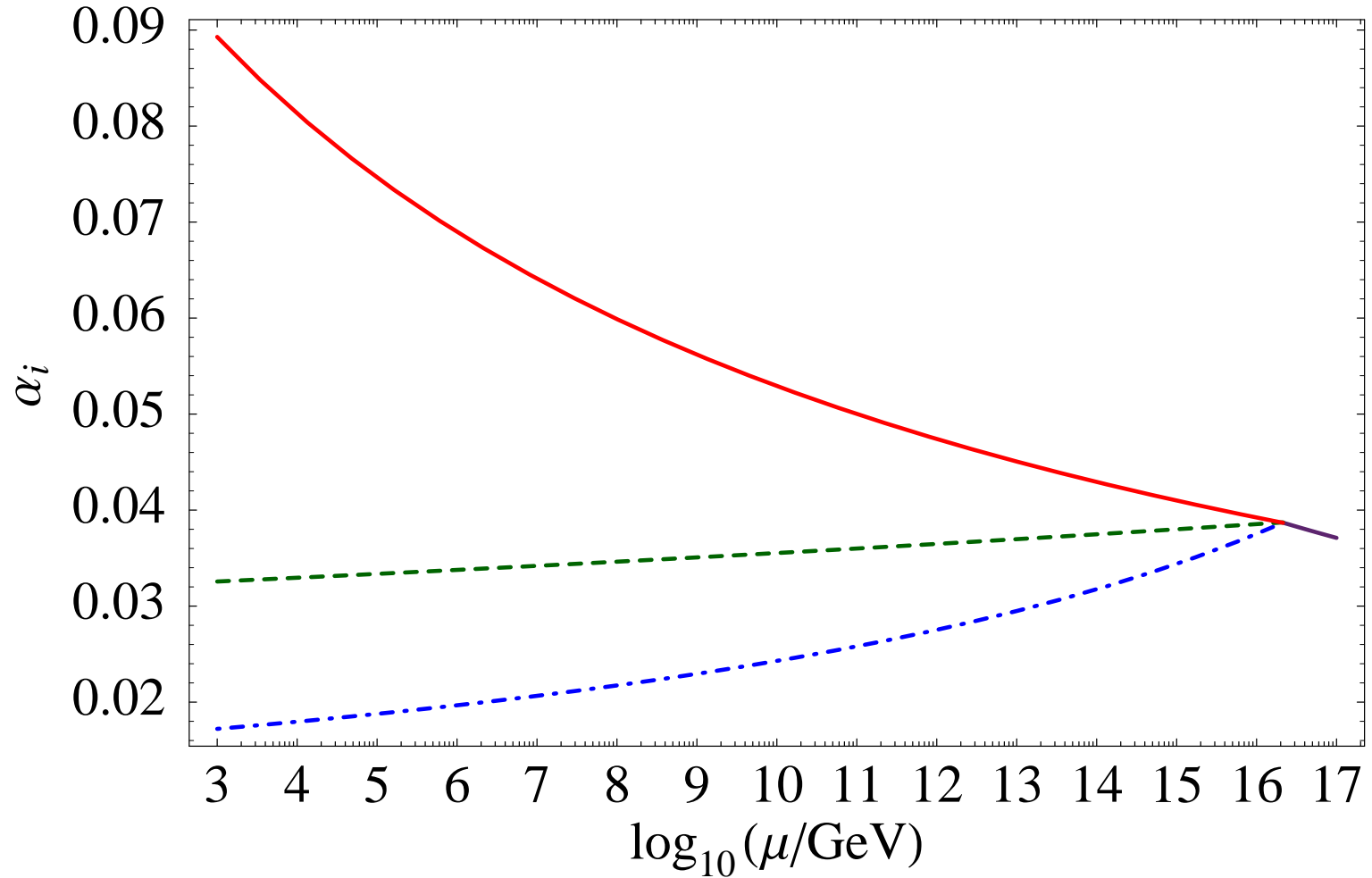
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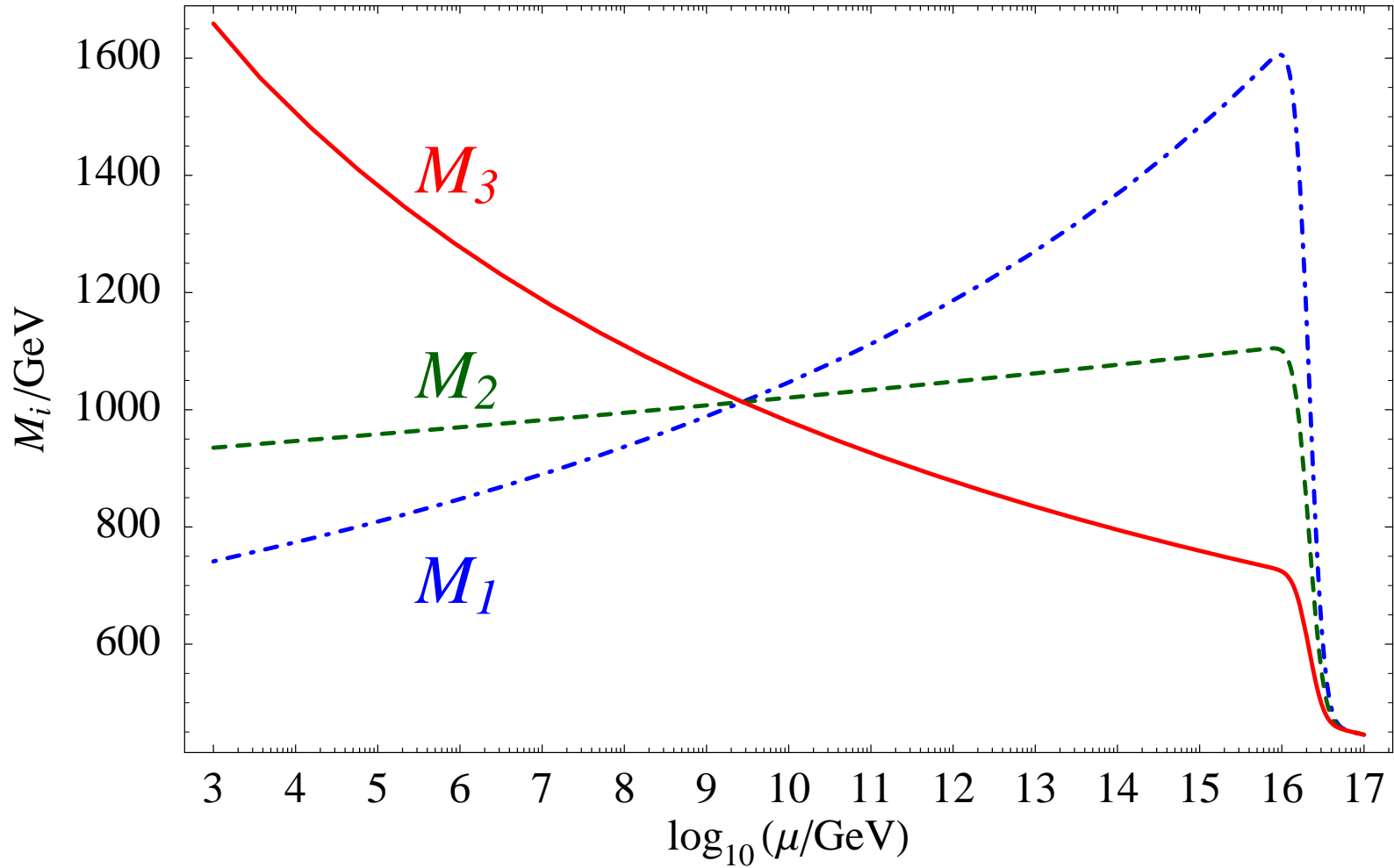
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The fact that we do not see supersymmetric particles at the LHC does not imply that Susy is absent. It is due to the fact that we have **more supersymmetry** than originally thought.

# Back up: Evolution of couplings



# The Mirage Scale



(Lebedev, HPN, Ratz, 2005)

# Reading the Gaugino Code

Mixed boundary conditions at the GUT scale characterized by the **parameter  $\alpha$** :  
the ratio of modulus to anomaly mediation.

- $M_1 : M_2 : M_3 \simeq 1 : 2 : 6$  for  $\alpha \simeq 0$
- $M_1 : M_2 : M_3 \simeq 1 : 1.3 : 2.5$  for  $\alpha \simeq 1$
- $M_1 : M_2 : M_3 \simeq 1 : 1 : 1$  for  $\alpha \simeq 2$
- $M_1 : M_2 : M_3 \simeq 3.3 : 1 : 9$  for  $\alpha \simeq \infty$

The mirage scheme leads to

- LSP  $\chi_1^0$  predominantly Bino
- a “compact” (compressed) gaugino mass pattern.

(Choi, HPN, 2007; Löwen, HPN, 2009)

# Gauginos Masses

